

Self-Diffusion Coefficients in the Molten AgNO_3 - AlkNO_3 Systems

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(Z. Naturforsch. **29 a**, 497–502 [1974] ; received 14 August 1973)

The cationic self-diffusion coefficients in the fused $(\text{Ag-Li})\text{NO}_3$, $(\text{Ag-Rb})\text{NO}_3$ and $(\text{Ag-Cs})\text{NO}_3$ systems have been investigated as a function of composition and temperature. The deviation from linearity of the D_+ vs. composition isotherms in the $(\text{Ag-Alk})\text{NO}_3$ series is discussed in terms of ionic interactions. Quantitative relationships between D_+ and ionic size and mass have been established.

Our preliminary results¹ on the cationic self-diffusion coefficients in $(\text{Ag-Alk})\text{NO}_3$ systems have proved their dependence on the ionic parameters which characterize the diffusing species. In order to establish the relation which expresses quantitatively this dependence, in addition to the previously studied $(\text{Ag-Na})\text{NO}_3$ and $(\text{Ag-K})\text{NO}_3$ mixtures¹ the remaining systems of the series, for which no data are available in literature: $(\text{Ag-Li})\text{NO}_3$, $(\text{Ag-Rb})\text{NO}_3$ and $(\text{Ag-Cs})\text{NO}_3$ have been investigated. The results concerning the self-diffusion coefficients of both cations (except D_{Li^+} whose isotope can not be identified by the technique presently used) as a function of composition and temperature are reported in the following.

Experimental Results

The “diffusion into the capillary” method previously described^{1, 2} has been used for the measurements. The nitrates were the same reagent grade quality as those used in our earlier works^{1, 2}. $^{110}\text{Ag}^+$, $^{86}\text{Rb}^+$ and $^{134}\text{Cs}^+$ were used as tracers. For each system the self-diffusion coefficients of both cations were measured over the entire concentration range from pure AgNO_3 to pure alkali nitrate at temperatures ranging from 240 to 400°. The experimental results are listed in Table 1–3.

In Table 4 are given the Arrhenius equation parameters (D_0 and E_D^+) for the self-diffusion coefficients as determined by the least squares method. The data for single AgNO_3 , RbNO_3 , and CsNO_3 in Table 4 are taken from our previous paper on pure nitrates². The diffusion coefficients of silver in the $(\text{Ag-Li})\text{NO}_3$ system can, within experimental errors ($\pm 4\%$), equally well be represented by a linear temperature dependence as by an Arrhenius equation.

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Table 1. Self-diffusion coefficient of Ag^+ in molten $(\text{Ag-Li})\text{NO}_3$ system.

x_{AgNO_3}	$T\text{ }^\circ\text{C}$	$D_{\text{Ag}^+} \cdot 10^5, \text{cm}^2 \cdot \text{sec}^{-1}$
0.75	232	1.12 ± 0.03
	266	1.39 ± 0.01
	307	1.70 ± 0.05
	330	1.88 ± 0.03
	343	1.99 ± 0.02
0.50	288	1.18 ± 0.01
	301	1.32 ± 0.01
	315	1.44 ± 0.03
	323	1.50 ± 0.02
0.25	288	1.42 ± 0.04
	302	1.58 ± 0.05
	328	1.92 ± 0.05
	336	2.05 ± 0.04
	350	2.21 ± 0.02

Table 2. Self-diffusion coefficients of Ag^+ and Rb^+ in molten $(\text{Ag-Rb})\text{NO}_3$ system.

x_{AgNO_3}	$T\text{ }^\circ\text{C}$	$D_{\text{Ag}^+} \cdot 10^5, \text{cm}^2 \cdot \text{sec}^{-1}$	$T\text{ }^\circ\text{C}$	$D_{\text{Rb}^+} \cdot 10^5, \text{cm}^2 \cdot \text{sec}^{-1}$
0.75	270	1.33 ± 0.05	292	1.42 ± 0.01
	294	1.62 ± 0.02	293	1.43 ± 0.02
	300	1.65 ± 0.01	328	1.77 ± 0.07
	305	1.78 ± 0.04	343	2.06 ± 0.03
	328	1.88 ± 0.03	384	2.64 ± 0.02
0.50	313	1.37 ± 0.02	277	1.04 ± 0.03
	324	1.48 ± 0.03	304	1.39 ± 0.02
	331	1.57 ± 0.04	309	1.34 ± 0.03
	355	1.82 ± 0.02	342	1.70 ± 0.01
0.25	304	1.18 ± 0.01	304	0.99 ± 0.01
	331	1.41 ± 0.01	313	1.14 ± 0.01
	341	1.50 ± 0.01	334	1.29 ± 0.03
	349	1.64 ± 0.04	345	1.45 ± 0.02
			362	1.57 ± 0.03

Discussion

When the dependence of self-diffusion coefficients on composition is studied, some regularities are evident.



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becomes larger. The hindrance occurring in the silver ion diffusion (Fig. 1) when AgNO_3 is added to an alkali nitrate melt, becomes more marked as the radius of the alkali cation increases, thus indicating an increase of ionic interaction in the K, Rb, Cs, sequence. The same is suggested by the maximum observed on the $E_D^{\text{Ag}^+}$ vs. composition curves (Figure 1). In Fig. 1, at the mol fraction $x_{\text{AgNO}_3} \approx 0$, we have used the interdiffusion coefficient data given by Sternberg and Herdlicka^{3,4}. The value $D_{\text{Ag}^+}^{\text{inter}}$ in CsNO_3 at 350° was calculated by extrapolating the experimental results beyond their temperature range. For completeness, our earlier data¹ for $(\text{Ag-Na})\text{NO}_3$ and $(\text{Ag-K})\text{NO}_3$ are also given in Figure 1.

For the alkali cations, a smooth dependence of D_{Me^+} on composition is observed (Fig. 2) and a systematical increase of the self-diffusion coefficient takes place as the composition of the melt is changing from pure MeNO_3 to pure AgNO_3 .

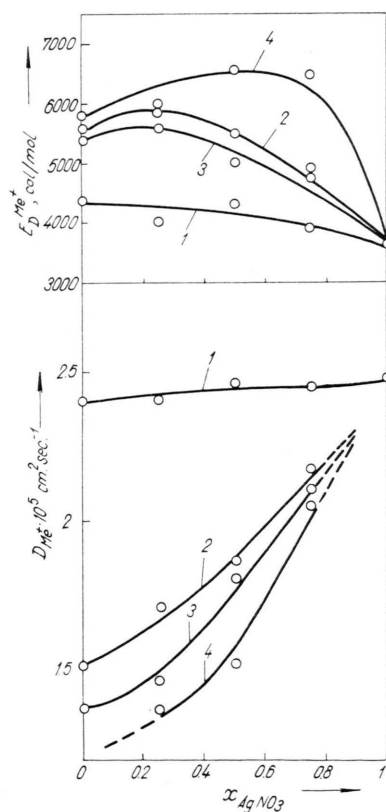


Fig. 2. Diffusion coefficient of alkali cation (Me^+) and activation energy vs. composition in $(\text{Ag-Alk})\text{NO}_3$ at 350° : 1) $(\text{Ag-Na})\text{NO}_3$; 2) $(\text{Ag-K})\text{NO}_3$; 3) $(\text{Ag-Rb})\text{NO}_3$; 4) $(\text{Ag-Cs})\text{NO}_3$.

The diffusion coefficient of Na^+ in pure AgNO_3 in Fig. 2 is the value of Sjöblom et al.⁵. For the other alkali ions there are no similar data in literature but, from the shape of the isotherms in Fig. 2 it appears that when $x_{\text{AgNO}_3} \rightarrow 1$, $D_{\text{Me}^+}^{\text{inter}}$ becomes the same for all the alkali ions. From the interdiffusion data in alkali nitrates in literature^{6,7} we have ascertained that this trend is not accidental but a rule which is convincingly proved by the data in Table 5.

Table 5. Interdiffusion coefficients of alkali cations in fused alkali nitrates.

Solvent	450° $D_{\text{Me}^+}^{\text{inter}} \cdot 10^5, \text{cm}^2 \cdot \text{sec}^{-1}$	Literature
NaNO_3	D_{K^+} 3.39	Honig ⁷
	D_{Rb^+} 3.28	Honig ⁷
	D_{Cs^+} 3.13	Kwak ⁶
KNO_3	D_{Na^+} 2.75	Honig ⁷
	D_{Rb^+} 2.83	Honig ⁷
	D_{Cs^+} 2.66	Honig ⁷
RbNO_3	D_{Na^+} 1.87	Honig ⁷
	D_{K^+} 2.13	Honig ⁷
	D_{Cs^+} 2.26	Kwak ⁶
CsNO_3	D_{Na^+} 2.41	Kwak ⁶
	D_{K^+} 2.44	Kwak ⁶
	D_{Rb^+} 2.32	Kwak ⁶

The special position of the $(\text{Ag-Na})\text{NO}_3$ system in the $(\text{Ag-Alk})\text{NO}_3$ series was already discussed¹. We mention here that a similar linear dependence on concentration was observed for the interdiffusion coefficient measured by a gravimetric method⁵ in the entire concentration range. Surprisingly, the more recent data on the interdiffusion coefficient obtained by the diaphragme cell method⁸ show a minimum on the D^{inter} vs. composition curve, that we think is difficult to explain.

Since it is generally accepted^{2,3,9-11} that Na^+ and Ag^+ in their molten nitrates are of similar ionic size, it is evident that in the $(\text{Ag-K,Rb,Cs})\text{NO}_3$ mixtures, the smaller cation is the Ag^+ ion. Accordingly, from Figs. 1 and 2, the following regularities become evident: on mixing, the self-diffusion coefficient of the smaller cation decreases as compared with its pure salt, while it increases for the larger cation. This recalls the similar concentration dependence of cationic mobilities^{6,7,12,13}. Due to the approximate relationship existing between the two transport parameters, $D_i = k T u_i$, the above behaviour can be assigned to the same reasons. As

for the ionic mobilities¹³, Lumsden's anion polarization model¹⁴ provides a satisfactory explanation. According to this model, due to the different size and induced polarizability of the two cations in the melt, some changes in cation-anion bond energy take place on mixing:

- a strengthening of the attractive force between the smaller cation and the common anion causing a decrease in the diffusion coefficient of the smaller ion;
- a weakening of the larger cation-common/anion bond energy, allowing some slight increase in diffusion coefficient of the larger ion.

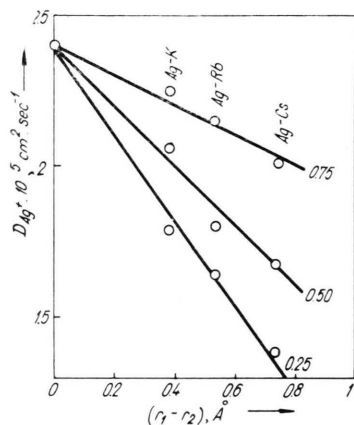


Fig. 3. Dependence of self-diffusion coefficient of Ag^+ on the $(r_1 - r_2)$ difference.

Our preliminary results¹ have shown that a definite relationship exists between the diffusion coefficient and the crystal radii of ions in the melt. As seen in Fig. 3 for each mol fraction there is a linear dependence of D_{Ag^+} on the difference of cationic radii. The equation of the straight lines ion Fig. 3,

calculated by the least squares method is:

$$D_{\text{Ag}^+} = D_{\text{Ag}^+}^0 - (1.946 \pm 0.243) \cdot 10^3 (r_1 - r_2) \cdot (1 - x_{\text{AgNO}_3}) \quad (1)$$

where $D_{\text{Ag}^+}^0$ stands for the self-diffusion coefficient of Ag^+ in fused AgNO_3 at the considered temperature and r_1 and r_2 are the cationic radii in cm.

A similar linear relationship also holds for D_{Me^+} :

$$D_{\text{Me}^+} = a - (1.964 \pm 0.335) \cdot 10^3 (r_1 - r_2) x_{\text{MeNO}_3} \quad (2)$$

If we take in (2) $x_{\text{MeNO}_3} \cong 0$ the self-diffusion coefficient of the alkali cation represents just its interdiffusion coefficient in fused AgNO_3 and we have:

$$D_{\text{Me}^+} = D_{\text{Me}^+}^{\text{inter}} = a.$$

When $x_{\text{MeNO}_3} = 1$, D_{Me^+} expresses the self-diffusion coefficient of the Me^+ cation in fused MeNO_3 so that:

$$D_{\text{Me}^+} = D_{\text{Me}^+}^0 = a - (1.964 \pm 0.335) \cdot 10^3 (r_1 - r_2)$$

and consequently, we may also write instead of (2) the following equation:

$$D_{\text{Me}^+} = D_{\text{Me}^+}^0 + (1.964 \pm 0.335) \cdot 10^3 (r_1 - r_2) \cdot (1 - x_{\text{MeNO}_3}) \quad (3)$$

which has a similar form with (1).

An alternative correlation could be established if we think that a mass effect should be observed in diffusion. Recently McDonald and Davis¹⁵ have expressed some excess transport properties, i. e. viscosity and thermal conductivity, in terms of the mass differences of the two cations, using the rigid elastic sphere model¹⁶.

Similarly, on the basis of the mass dependence of the diffusion coefficient from the kinetic theory of diffusion¹⁷, we have assumed a linear dependence of

D_{Ag^+} on $\left(\frac{m_1 + m_2}{m_1 m_2}\right)^{1/2}$. As a consequence the self-

Table 6. Calculated and experimental self-diffusion coefficients in fused $(\text{Ag-Alk})\text{NO}_3$ systems, at 350° .

System	x_{AgNO_3}	$D_{\text{Ag}^+} \cdot 10^5, \text{cm}^2 \cdot \text{sec}^{-1}$				$D_{\text{Me}^+} \cdot 10^5, \text{cm}^2 \cdot \text{sec}^{-1}$	
		D_{exp}	D_c Eq. (1)	D_c Eq. (4)	D_c Eq. (5)	D_{exp}	D_c Eq. (3)
$(\text{Ag-K})\text{NO}_3$	0.75	2.25	2.21	2.17	2.21	2.22	2.17
	0.50	2.06	2.03	1.88	2.04	1.87	1.88
	0.25	1.79	1.85	1.60	1.87	1.72	1.70
$(\text{Ag-Rb})\text{NO}_3$	0.75	2.15	2.14	2.16	2.13	2.12	2.15
	0.50	1.80	1.88	1.86	1.88	1.82	1.89
	0.25	1.64	1.63	1.56	1.63	1.47	1.53
$(\text{Ag-Cs})\text{NO}_3$	0.75	2.01	2.04	2.15	2.02	2.05	—
	0.50	1.68	1.68	1.84	1.67	1.52	—
	0.25	1.37	1.32	1.54	1.31	1.38	—

diffusion coefficients could be expressed as:

$$D_{\text{Ag}^+} = D_{\text{Ag}^+}^0 - (1.405 \pm 0.454) \cdot \left[1 - \left(\frac{m_{\text{Ag}} + m_{\text{Me}}}{m_{\text{Ag}} m_{\text{Me}}} \right)^{1/2} \right] (1 - x_{\text{AgNO}_3}) \quad (4)$$

From (1) and (4) it follows that D_{Ag^+} can also be written as:

$$D_{\text{Ag}^+} = D_{\text{Ag}^+}^0 - (2.204 \pm 0.28) \cdot 10^3 \cdot \left[1 - \left(\frac{m_{\text{Ag}} + m_{\text{Me}}}{m_{\text{Ag}} m_{\text{Me}}} \right)^{1/2} \right] (r_1 - r_2) (1 - x_{\text{AgNO}_3}) \quad (5)$$

The ability of (1), (3), (4) and (5) to predict the experimental results is given in Table 6. All in all, the data in Table 6 suggest that the cationic masses are probably as important as the differences in cationic radii in determining the diffusion coefficient. However the best fit with experimental results is given by Equation (1).

An attempt has been made to apply the above relationships to other data available in literature. It has been found that the experimental results are always given within experimental error by an equation of the form (1) when the smaller cation in the mixture is concerned and (3) for the larger one. The numerical value of the slope in (1) and (3) varies with the considered solvent. Table 7 illustrates the results for the $(\text{Na-K})\text{NO}_3$ and $(\text{Na-Cs})\text{NO}_3$ systems. The experimental results in Table 7 are those given by Lantelme¹² for

Table 7. Calculated and experimental self-diffusion coefficients in fused $(\text{Na-K})\text{NO}_3$ and $(\text{Na-Cs})\text{NO}_3$ systems.

System	x_{NaNO_3}	$D_{\text{Na}^+} \cdot 10^5, \text{cm}^2 \cdot \text{sec}^{-1}$		$D_{\text{Me}^+} \cdot 10^5, \text{cm}^2 \cdot \text{sec}^{-1}$		$T, ^\circ\text{C}$
		D_{exp}	D_{c}	D_{exp}	D_{c}	
$(\text{Na-K})\text{NO}_3$	0.75	2.14	2.21	1.82	1.79	350
	0.50	2.06	2.03	1.75	1.69	
	0.25	1.95	1.84	1.64	1.59	
$(\text{Na-Cs})\text{NO}_3$	0.75	3.50	3.37	2.80	2.82	450
	0.50	3.18	3.04	2.57	2.64	
	0.25	2.95	2.91	2.35	2.45	

$(\text{Na-K})\text{NO}_3$ and by Kwak⁶ for $(\text{Na-Cs})\text{NO}_3$. It is worthnoting that the D_{c} data for the Na^+ ion were calculated by (1) without changing the numerical values of intersection and slope. The good agreement with the experimental results in both systems indicates, once more, the similarity of the ionic sizes of Ag^+ and Na^+ ions in their molten nitrates.

None of the above mentioned regularities fit the $(\text{Ag-Li})\text{NO}_3$ mixtures. As seen in Fig. 4, the D_{Ag^+}

vs. composition curves show a peculiar behaviour in comparison with the other systems of the series: significant deviations from additivity with a very pronounced minimum at equimolecular composition.

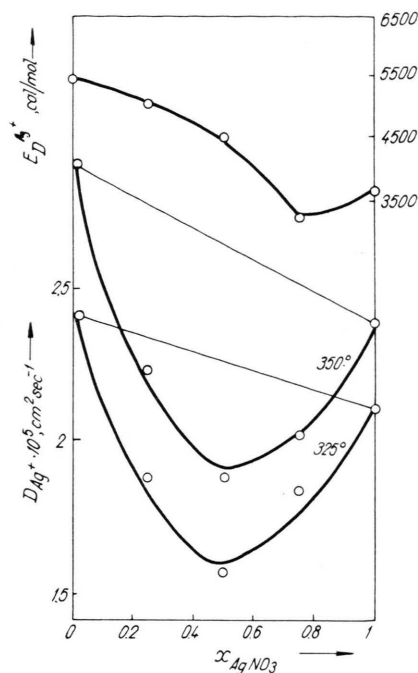


Fig. 4. Diffusion coefficients isotherms of Ag^+ ion and activation energy vs. composition in $(\text{Ag-Li})\text{NO}_3$ system.

A similar dependence on composition is also shown by interdiffusion coefficients⁸. The peculiarity of this system is also evident from the minimum shown on the $E_D^{\text{Ag}^+}$ vs. composition plot, never observed for the other systems of the series. In Fig. 4 the literature data^{3, 18} were used for $D_{\text{Ag}^+}^{\text{inter}}$ in LiNO_3 and $E_D^{\text{Li}^+}$ respectively. The magnitude of the deviations in Fig. 4 are too large to be caused by simple competitive interionic attractions. The observed effect may be due to some other factors such as closer packing or eutectic formation (as indicated by phase diagram^{19, 20}) caused by the strong polarization exerted by the Li^+ ion.

Surprisingly, the recent Raman Spectra²¹ indicate that, apart from changes in intensity, the librational bands are essentially unaffected in the $(\text{Ag-Li})\text{NO}_3$ system, which implies no essential structural changes on mixing. This is not confirmed by the diffusion data.

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